On simple linear recurrences

Andrzej Schinzel

Let K be a number field and u_n a simple linear recurrence of order k defined over K. We shall consider for $k = 2, 3, 4$ the following problem: if for almost all prime ideals p of K there are elements u_n divisible by p, does it follow that $u_n = 0$ for a certain integer n?